

In search of the Minsky moment

M. R. Grasselli

Introduction

Asset Price Bubbles

Banks

Modelling Minsky

In search of the Minsky moment

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Outline

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Dynamic General Equilibrium views

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- Seek to explain the aggregate economy using theories based on strong microeconomic foundations.
- Collective decisions of rational individuals over a range of variables for both present and future.
- All variables are assumed to be simultaneously in equilibrium.
- The only way the economy can be in disequilibrium at any point in time is through basing decisions on wrong information.
- Money is neutral in its effect on real variables.
- Largely ignore uncertainty by simply subtracting risk premia from all risky returns and treat them as risk-free.



Minsky's alternative interpretation of Keynes

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- Neoclassical economics is based on barter paradigm: money is convenient to eliminate the double coincidence of wants.
- In a modern economy, firms make complex portfolios decisions: which assets to hold and how to fund them.
- Financial institutions determine the way funds are available for ownership of capital and production.
- Uncertainty in valuation of cash flows (assets) and credit risk (liabilities) drive fluctuations in real demand and investment.
- Economy is fundamentally cyclical, with each state (boom, crisis, deflation, stagnation, expansion and recovery) containing the elements leading to the next in an identifiable manner.



Minsky's Financial Instability Hypothesis

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- Start when the economy is doing well but firms and banks are conservative (perhaps because of memory of previous crisis).
- Most projects succeed "Existing debt is easily validated and units that are heavily in debt prospered: it pays to lever".
- Revised valuation of cash flows, exponential growth in credit, investment and asset prices.
- Highly liquid, low-yielding financial instruments are devalued, rise in corresponding interest rate.
- Beginning of "euphoric economy": increased debt to equity ratios, development of Ponzi financier.
- Viability of business activity is eventually compromised.
- Ponzi financiers have to sell assets, liquidity dries out, asset market is flooded.
- Euphoria becomes a panic.



Defintion

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Modelling Minsky • Consider a representative agent solving

$$\sup_{c} E_t \left[\sum_{j=1}^{\infty} \beta^{j-t} u(c_j) \right]$$

for exogenously given (e_t, d_t) .

• Denoting $q_t = u'(e_t + d_t)p_t$, the FOC for optimality give

$$q_t - \beta E_t [q_{t+1}] = \beta E_t [d_{t+1}u'(e_{t+1} + d_{t+1})]$$

• The general solution is of the form $q_t = F_t + B_t$ where

$$F_t = \sum_{j=1}^{\infty} \beta^j E_t \left[d_{t+j} u' (e_{t+j} + d_{t+j}) \right]$$

is the fundamental price and B_t is a bubble term satisfying $E_t[B_{t+1}] = \beta^{-1}B_t$ (1)



Consequences

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- $B_t \ge 0$ for all t.
- Any nonzero rational bubble must start with $B_0 > 0$.
- If $T < \infty$, $B_t = 0$ for all $0 \le t \le T$, and this result is robust with respect to diverse information (Tirole 1982).
- If *T* = ∞, bubbles can exit in a myopic rational expectations equilibrium.
- Rational bubbles cannot exist in a fully dynamic REE with finitely many infinitely lived agents.
- They can exit in an overlapping generations models provided 0 < r

 g, where r
 is the asymptotic real interest rate and g is the rate of growth of the economy (Tirole 1985).



The Efficient Markets Hypothesis

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- Denote $R_{t+1} = \frac{p_{t+1} p_t + d_{t+1}}{p_{t+1}}$.
- As we have seen, a first-order rational expectations condition for risk-neutral agents leads to

$$E_t[R_{t+1}] = 1 + r.$$
 (2)

• Solving this recursively leads to

$$p_t = \sum_{j=1}^{\infty} \frac{1}{(1+r)^j} E_t[d_{t+j}],$$
(3)

plus a possible rational bubble term satisfying $E_t[B_{t+1}] = (1+r)B_t$.

- Either (2) or (3) can be taken as an EMH.
- Statistical tests on actual returns indicate that they are not *very* forecastable, leading to the conclusion that the EMH cannot be rejected.



Volatility bounds

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- Suppose that $p_t = E_t[p_t^*]$, where p_t^* is a perfect foresight price.
- Then $p_t^* = p_t + \varepsilon_t$, where ε_t is the forecast error and is uncorrelated with p_t .
- It follows that $\sigma(p_t) \leq \sigma(p_t^*)$.
- This, however, is found to be dramatically violated by data (Shiller 1981).



Violation of Volatility Bounds

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Figure 1

Note: Real Standard and Poor's Composite Stock Price Index (solid line p) and ex posr rational price (dotted line p), 1871–1979, both detrended by dividing a longrun exponential growth factor. The variable p^* is the present value of actual subsequent real detrended dividends, subject to an assumption about the present value in 1979 of dividends thereafter. Data are from Data Set 1, Appendix.



FIGURE 2

Note: Real modified Dow Jones Industrial Average (solid line p) and ex post rational price (dotted line p^*), 1928-1979, both detrended by dividing by a long-run exponential growth factor. The variable p^* is the present value of actual subsequent real detrended dividends, subject to an assumption about the present value in 1979 of dividends thereafter Data are from Data Set 2, Appendix.

Figure: Source: Shiller (1981)



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Alternative models (Shiller, 1984)

• Consider a model where sophisticated investors have a demand function (portion of shares) of the form

$$Q_t^i = \frac{E_t[R_{t+1}] - \alpha}{\phi}.$$
 (4)

- In addition, suppose there are noise traders who react to fads Y_t through a demand function $Q_t^n = Y_t/p_t$.
- In equilibrium we have $Q_t + \frac{Y_t}{p_t} = 1$.
- Inserting this into (4) and solving recursively leads to

$$p_t = \sum_{j=1}^{\infty} \frac{E_t[d_{t+j}] + \phi E_t[Y_{t-1+j}]}{(1+\alpha+\phi)^j}.$$
 (5)

• This is also consistent with prices being not very forecastable.



Other sources of inefficiencies

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- Noise trader risk (DeLong, Shleifer, Summers and Waldmann 1990): prices deviate from fundamental value because of uncertainty created by noise traders, who can in some cases earn higher expected returns than sophisticated investors.
- Limits of arbitrage (Shleifer and Vishny 1997): performance based arbitrage lead to fund managers leaving the market exactly when they are needed to restore fundamental value.
- No short-sales and diverse beliefs (Miller 1977, Harrison and Kreps 1978): pessimists sit on sidelines and optimists overbid leading to prices higher than fundamentals.
- Overconfidence (Scheinkman and Xiong 2003): mean reverting confidence levels lead to prices that contain an option to re-sell the asset at a later time.



Financial Intermediation (Allen and Gale, 2000)

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- Suppose there is a continuum of small, risk-neutral investors with no wealth of their own and a continuum of small, risk-neutral banks with B > 0 funds to lend at rate r trading at t = 1, 2.
- Consider a safe asset (s) with return (1 + r) and a risky asset (R) with price at t = 2 given by a random variable p₂ with density h(p₂) on [0, p₂^{max}] and mean p₂.
- In addition, there is a production function f(x) for the economy and an investment cost c(x).



Existence of bubbles

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- A representative investor needs to choose quantities Q₁^s and Q₁^R of the safe and unsafe assets at time t = 1 at prices 1 and p₁, respectively.
- The equilibrium price in the presence of banks is then

$$p_1 = \frac{1}{1+r} \left[\frac{\int_{(1+r)p_1}^{p_2^{\max}} p_2 h(p_2) dp_2 - c'(1)}{\Prob[p_2 \ge (1+r)p_1]} \right].$$
(6)

- Define the fundamental value as the price that an investor would pay if he had to use his own money B > 0.
- This leads to

$$p_1^F = \frac{\overline{p_2} - c'(1)}{1 + r}.$$
 (7)

• We can then show that $p_1 \ge p_1^F$ with strict inequality iff $\operatorname{Prob}[p_2 < (1+r)p_1] > 0$



Liquidity preferences

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- An asset is illiquid if its liquidation value at an earlier time is less than the present value of its future payoff.
- For example, an asset can pay $1 \le r_1 \le r_2$ at dates T = 0, 1, 2.
- Let $(r_1 = 1, r_2 = R)$ be an illiquid asset and $(r_1 > 1, r_2 < R)$ be a liquid one.
- At time *t* = 0, consumers don't know in which future date they will consume.
- The expected utility for consumers is

$$pU(r_1) + (1-p)U(r_2),$$

where p is the proportion of early consumers.

- Sufficiently risk-averse consumers prefer the liquid asset.
- A similar story holds for entrepreneurs.



A model for a bank, Diamond and Dybvig (1983)

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- Banks borrow short and lend long.
- Suppose a bank offers a liquid asset $(r_1 = 1.28, r_2 = 1.813)$ to 100 depositors each with \$1 at t = 0.
- In addition, the bank can invest in an illiquid asset $(r_1 = 1, r_2 = 2)$.
- If w = 1/4, the bank needs to pay $25 \times 1.28 = 32$ at t = 1.
- At t = 2 the remaining depositors receive $\frac{68 \times 2}{75} = 1.813$ and the bank is solvent.
- This is a Nash equilibrium is *all* depositors expect only 25 to withdraw at *t* = 1.
- *But* liquidity preferences are unverifiable private information.
- Another Nash equilibirum consisting of *all* depositors forecasting that everyone will withdraw at *t* = 1.



Our model - the summarized story

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- Liquidity Preference
- Searching for partners
- Learning and Predicting
- Bank birth
- Interbank Links
- Contagion



Society

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Liquidity preferences Bank formation

- We have a society of individuals investing at the beginning of each period (t = 0).
- For each individual *i*, an initial preference is drawn from a continuous uniform random variable U_i : the investor is deemed to have short term liquidity preferences if $U_i < 0.5$ and long term liquidity preferences otherwise.
- There is a shock to their preferences at the middle of the period (*t* = 1).
- If the shock is big enough the individual would have wished he made his investment differently.
- At time t = 1, $W_i = \left| \frac{U_i + (-1)^{ran_i} \epsilon_i}{2} \right|$
- If $W_i < 0.5$ the investor wants to become a short term investor, otherwise he wants to be long term investor
- Because of anticipated shocks, individuals explore the society searching to partners to exchange investments.



Searching for partners

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- We impose some constrains on the individual capacity to go around and seek other individuals to trade.
- This reflects the inherited limited capability of information gathering and environment knowledge of individual agents.
- We use a combination of von Neumann and Moore neighborhoods:
 - 5 1 6 2 X 3
 - 7 4 8



To join or not to join a bank

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- Assume a bank offers a fixed contract promising a payment of $c_1 > 1$ at t = 1 for each unit (dollar) deposited and $1 < c_2 < R$ for t = 2 under the assumption there is no bank run.
- Then agents will join the bank if they have:
 - short term preferences and expect not to change preferences in the next period
 - Short term preferences, expect to change preference and not find a partner to trade
 - Iong term preferences and expects to change preference
- Agents will not join the bank if they have:
 - short term preferences, expect to change and believes he can find a partner
 - Ong term preferences and are confident they will not change



Bank birth

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- We follow the work of Howitt and Clower (1999,2007) on the emergence of economic organizations
- With probability 0 < h < 1 an agent will have the 'idea of entrepreneurship'
- Market search for an opportunity to establish a bank
- Establish a bank if he can find x and y such that $x + y \le 1$ and

$$y = c_1 W_i$$
$$Rx = c_2 (1 - W_i)$$

- Individuals become aware of bank existence only if the bank lies in their neighbourhood.
- In addition we give the bank the reach of its new members.



Experiment: bank formation

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Experiment (continued): established banks



Figure: Banks at T=100 with h = 0.9, $c_1 = 1.1$, $c_2 = 1.5$ and R = 2.



Experiment (continued): number of depositors



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Next steps

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- Need to incorporate bank run
- Individuals moving between banks
- Banks form a new kind of agents that can in turn trade with each other to distribute the risk of asymmetric liquidity shocks a la Allen and Gale (2000):



Figure: Networks, complete connected (left), incomplete connected (middle), incomplete disconnected (right)



Goodwin's Model

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- Let $N = n_0 e^{\beta t}$ be the labour force, $a = a_0 e^{\alpha t}$ be its productivity and $\lambda = L/N$ be the employment rate.
- Define the total output Y = aL and total capital as $K = \nu Y$.
- Assume that wages satisfy

$$\frac{dw}{dt}=F_w(\lambda)w,$$

where $F_w(\lambda)$ is a Phillips curve.

- Let the wages share of total output be ω and profit share be $\pi=1-\omega.$
- Suppose further that the rate of new investment is given by

$$I = \frac{dK}{dt} = (1 - \omega)Y - \gamma K$$



Differential Equations

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Basic Goodwin's model Keen's model Ponzi financing • It is easy to deduce that this leads to

$$\frac{d\omega}{dt} = \omega(F_w(\lambda) - \alpha) \tag{8}$$

$$\frac{d\lambda}{dt} = \lambda \left(\frac{1-\omega}{\nu} - \alpha - \gamma - \beta \right)$$
(9)

• This system is globally stable and leads to endogenous cycles of employment.



Example 1: basic Goodwin model

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Example 1 (continued): basic Goodwin model

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Keen's extended model

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Basic Goodwin's model Keen's model Ponzi financing • Consider the same model as before, but with a nonlinear investment function $I_g = F_i(\pi_n)$ of the net profit share is

$$\pi_n = 1 - \omega - rd,$$

where d = D/Y and the absolute debt level D evolves according to

$$\frac{dD}{dt} = I_g - \pi_n = rD + F_i(\pi_n) - (1 - \omega)$$



Differential Equations

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Basic Goodwin's model Keen's model Ponzi financing • The corresponding dynamical systems now reads

$$\frac{d\omega}{dt} = \omega(F_w(\lambda) - \alpha) \tag{10}$$

$$\frac{d\lambda}{dt} = \lambda \left(\frac{F_i(\pi_n)}{\nu} - \alpha - \gamma - \beta \right)$$
(11)

$$\frac{dd}{dt} = F_i(\pi_n) - (1 - \omega) - d\left(\frac{F_i(\pi_n)}{\nu} - \gamma\right)$$
(12)

• This system is locally stable but globally unstable.



Example 2: convergent Goodwin model with banks

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Example 2 (continued): convergent Goodwin model with banks





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Example 3: divergent Goodwin model with banks

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Example 3 (continued): divergent Goodwin model with banks



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Basin of convergence for Goodwin model with banks



lambda



Ponzi financing

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Basic Goodwin's model Keen's model Ponzi financing • To introduce the destabilizing effect of purely speculative investment consider a modified version of the previous model with

$$\frac{dD}{dt} = I_g - \pi_n + P_k,$$

where

$$\frac{dP_k}{dt} = F_p(g)$$

 Here F_p(·) is a increasing nonlinear function of the growth rate of capital assets given by

$$g=\frac{F_i(\pi_n)}{\nu}-\gamma.$$



Effect of Ponzi financing



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Next steps

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- Add government (regulatory) sector.
- Model asset prices explicitly.
- Introduce noise (stochastic interest rates, risk premium, etc)
- Thanks !