

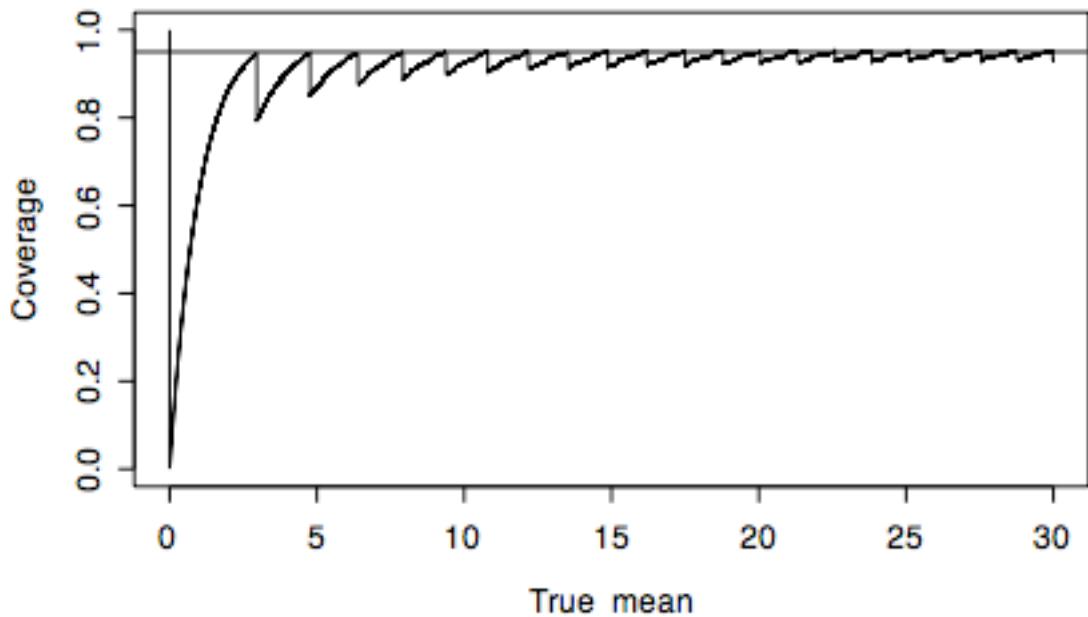
# STATS 4F03/6F03 Test #1 SOLUTIONS

## Part A

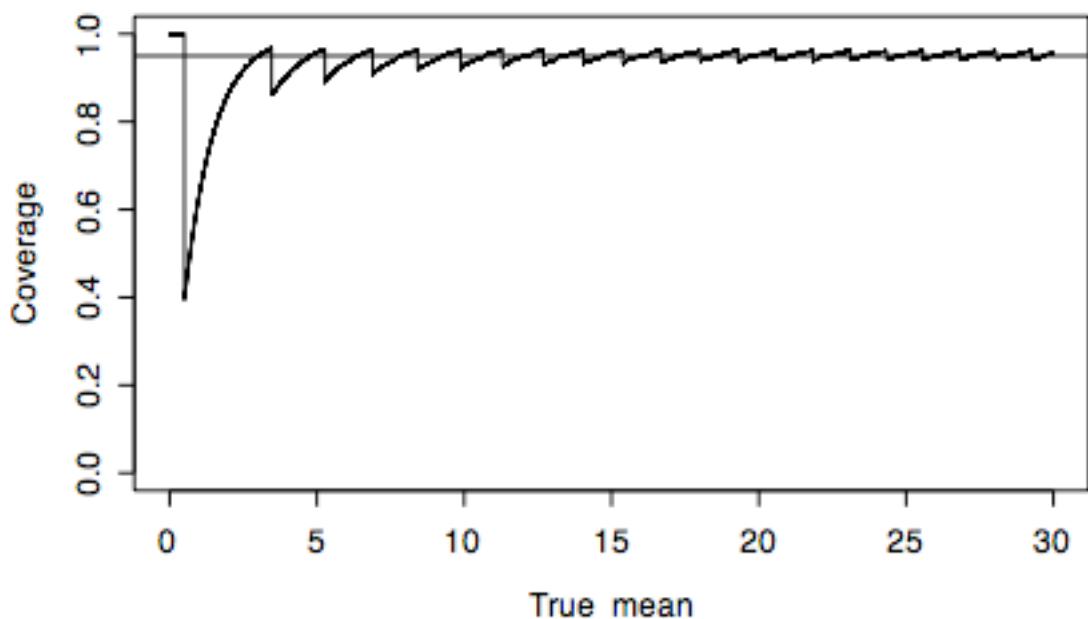
```
> coverplotpois <-
function (fun, mumax = 30, alpha = 0.05, by = 0.001, ...)
{
  mugr <- seq(0, mumax, by = by)
  plot(c(0, mumax), c(0, 1), type = "n", xlab = "True mean",
       ylab = "Coverage")
  abline(h = 1 - alpha)
  lines(mugr, sapply(mugr, fun), lty = 1)
  invisible()
}
> poisconfn0 <-
function (mu = 1, maxx = 500, alpha = 0.05)
{
  x <- (0:maxx)
  mulow <- x - qnorm(1 - alpha/2) * sqrt(x)
  muup <- x + qnorm(1 - alpha/2) * sqrt(x)
  sum(dpois(x, mu) [(mulow <= mu) & (muup >= mu)])
}
> poisconfn1 <-
function (mu = 1, maxx = 500, alpha = 0.05)
{
  x <- (0:maxx)
  mulow <- x - 0.5 - qnorm(1 - alpha/2) * sqrt(x)
  muup <- x + 0.5 + qnorm(1 - alpha/2) * sqrt(x)
  sum(dpois(x, mu) [(mulow <= mu) & (muup >= mu)])
}
> poisconfn2 <-
function (mu = 1, maxx = 500, alpha = 0.05)
{
  x <- (0:maxx)
  a <- qnorm(1 - alpha/2)
  mulow <- x + a^2/2 - a * sqrt(x + a^2/4)
  muup <- x + a^2/2 + a * sqrt(x + a^2/4)
  sum(dpois(x, mu) [(mulow <= mu) & (muup >= mu)])
}
> poisconfig <-
function (mu = 1, maxx = 200, alpha = 0.05)
{
  x <- (0:maxx)
  mulow <- qgamma(alpha/2, x + 0.5)
  muup <- qgamma(1 - alpha/2, x + 0.5)
  sum(dpois(x, mu) [(mulow <= mu) & (muup >= mu)])
}

> coverplotpois(poisconfn0, by=0.001)
> title(main="First normal approx, no cc")
> coverplotpois(poisconfn1, by=0.001)
> title(main="First normal approx with cc")
> coverplotpois(poisconfn2, by=0.001)
> title(main="Second normal approx, no cc")
> coverplotpois(poisconfig, by=0.005, maxx=300)
> title(main="Exact Poisson mid-P")
```

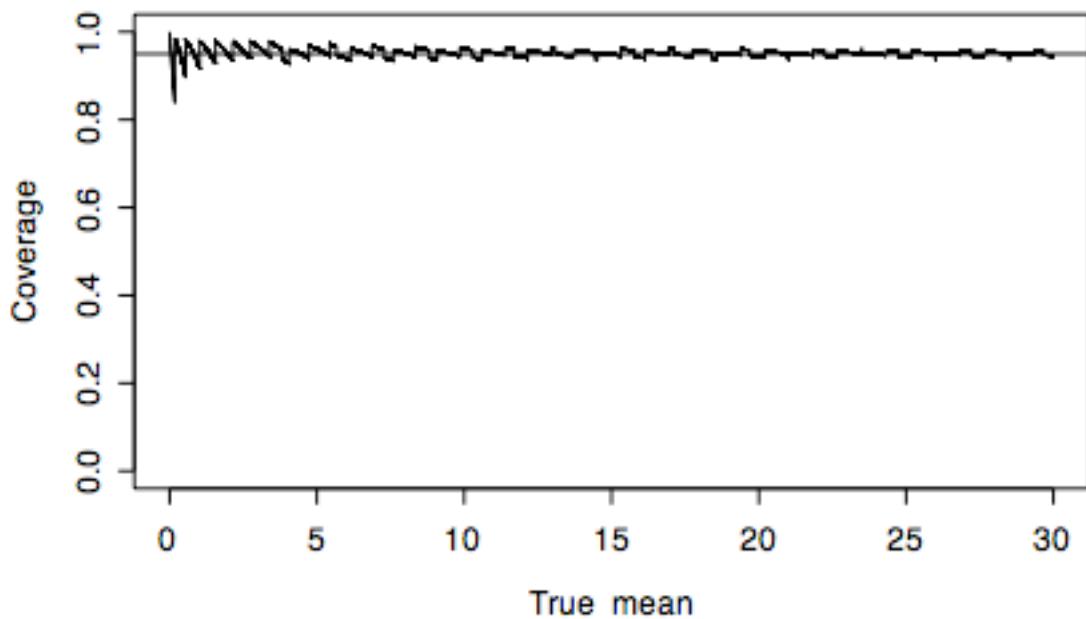
**First normal approx, no cc**



**First normal approx with cc**



Second normal approx, no cc



Exact Poisson mid-P

